

What you will learn about:  
Simplify and Use of Square Roots

Square Root of a Number:

If  $n^2 = m$ , then  $n$  is the square root of  $m$

Radical -  $\sqrt{\phantom{0}}$

Radicand – Number under the radical

$\sqrt{m}$  is read as "the square root of  $m$ ."

If  $m = n^2$ , then  $\sqrt{m} = n$ , for  $n \geq 0$ .

The square root of  $m$ ,  $\sqrt{m}$ , is the positive number whose square is  $m$ .

$\sqrt{1}$	$\sqrt{4}$	$\sqrt{9}$	$\sqrt{16}$	$\sqrt{25}$	$\sqrt{36}$	$\sqrt{49}$	$\sqrt{64}$	$\sqrt{81}$	$\sqrt{100}$	$\sqrt{121}$	$\sqrt{144}$	$\sqrt{169}$	$\sqrt{196}$	$\sqrt{225}$
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15

Simplify

$$\sqrt{36}$$

6

$$\sqrt{196}$$

14

$$-\sqrt{81}$$

-9

$$\sqrt{-121}$$

No Real  
Solutions

$$\sqrt{a} + \sqrt{b} \neq \sqrt{a+b}$$

$$\sqrt{25} + \sqrt{144}$$

$$5 + 12$$

$$17$$

$$\sqrt{25 + 144}$$

$$\sqrt{169}$$

$$13$$

$$7 = \sqrt{49}$$

$$8 = \sqrt{64}$$

$$\sqrt{36} = 6$$

$$\sqrt{49} = 7$$

### Estimating Square Roots

Estimate  $\sqrt{60}$  between two consecutive whole numbers.  
*between 7 and 8. Closer to 8.*

Estimate  $\sqrt{38}$  between two consecutive whole numbers.  
*between 6+7. Closer to 6.*

### Approximate Square Roots

Use your calculator to find  $\sqrt{5}$ . Round to the nearest hundredth.

2.24

Round  $\sqrt{58}$  to two decimal places.

7.62

### Simplifying Variable Expressions with Square Roots

$$\text{Find } \sqrt{9x^2} = (3x)^2 = 9x^2 \quad \sqrt{9x^2} = 3x$$

$$(?)^2 = 9x^2$$

$$(3x)^2 = 9x^2, \quad \text{so } \sqrt{9x^2} = 3x$$

$$\sqrt{25u^8} = 5u^4 \quad \text{because } (5u^4)^2 = 25u^8$$

$$\sqrt{16r^{20}} = 4r^{10} \quad \text{because } (4r^{10})^2 = 16r^{20}$$

$$\sqrt{196q^{36}} = 14q^{18} \quad \text{because } (14q^{18})^2 = 196q^{36}$$

Simplify:

$$\sqrt{x^6} = x^3$$

$$\sqrt{b^{10}} = b^5$$

$$\sqrt{64x^4}$$

$$\sqrt{36x^2y^8}$$

$$(x^4)^2 = x^8$$

$$8x^2$$

$$6xy^4$$

$$-\sqrt{100a^{10}}$$

$$-\sqrt{225x^4y^2}$$

$$\sqrt{49x^{30}}$$

$$\sqrt{121w^{36}}$$

$$-10a^5$$

$$-15x^2y$$

$$7x^{15}$$

$$11w^{18}$$

$$\sqrt{169x^{10}y^{14}}$$

$$\sqrt{144a^{16}b^{20}c^8}$$

$$13x^5y^7$$

$$12a^8b^{10}c^4$$

What you will learn about:  
Simplify Square Roots

Product Property of Square Roots

If  $a, b$  are non-negative real numbers, then  $\sqrt{ab} = \sqrt{a} \cdot \sqrt{b}$ .

Simplify a square root using the Product property.

**Step 1** – Find the largest perfect square of the radicand. Rewrite the radicand as a product using the perfect-square factor.

**Step 2** – Use the product rule to rewrite the radical as the product of two radicals.

**Step 3** – Simplify the square root of the perfect square.

$$\sqrt{ab} = \sqrt{a} \cdot \sqrt{b}$$

$$\sqrt{72} = \sqrt{4} \cdot \sqrt{8}$$

$$3\sqrt{8} = 3\sqrt{4} \cdot \sqrt{2}$$

$$3 \cdot 2 \cdot \sqrt{2}$$

Simplify:

$$\sqrt{50} = \sqrt{25} \cdot \sqrt{2}$$

$$5\sqrt{2}$$

$$\sqrt{500} = \sqrt{100} \cdot \sqrt{5}$$

$$10\sqrt{5}$$

$$\sqrt{48} = \sqrt{16} \cdot \sqrt{3}$$

$$4\sqrt{3}$$

$$\sqrt{288} = \sqrt{144} \cdot \sqrt{2}$$

$$12\sqrt{2}$$

$$\sqrt{45} = \sqrt{9} \cdot \sqrt{5}$$

$$3\sqrt{5}$$

$$\sqrt{72} = \sqrt{36} \cdot \sqrt{2}$$

$$6\sqrt{2}$$

$$\sqrt{x^3}$$

$$\sqrt{x^2} \cdot \sqrt{x}$$

$$x\sqrt{x}$$

$$\sqrt{b^5}$$

$$\sqrt{b^4} \cdot \sqrt{b}$$

$$b^2\sqrt{b}$$

$$\sqrt{p^9}$$

$$\sqrt{p^8} \cdot \sqrt{p}$$

$$p^4\sqrt{p}$$

$$\sqrt{16x^7}$$

$$\sqrt{16} \cdot \sqrt{x^7}$$

$$\sqrt{16} \cdot \sqrt{x^6} \cdot \sqrt{x}$$

$$4x^3\sqrt{x}$$

$$\sqrt{25y^5}$$

$$\sqrt{25} \cdot \sqrt{y^4} \cdot \sqrt{y}$$

$$5y^2\sqrt{y}$$

$$\sqrt{144t^{11}}$$

$$\sqrt{144} \cdot \sqrt{t^{10}} \cdot \sqrt{t}$$

$$12t^5\sqrt{t}$$

$$\sqrt{32y^5}$$

$$\sqrt{16} \cdot \sqrt{2} \cdot \sqrt{y^4} \cdot \sqrt{y}$$

$$4\sqrt{2} \cdot y^2\sqrt{y}$$

$$4y^2\sqrt{2y}$$

$$\sqrt{75a^9}$$

$$\sqrt{25} \cdot \sqrt{3} \cdot \sqrt{a^8} \cdot \sqrt{a}$$

$$5\sqrt{3} \cdot a^4\sqrt{a}$$

$$5a^4\sqrt{3a}$$

$$\sqrt{63u^3v^5}$$

$$\sqrt{9} \cdot \sqrt{7} \cdot \sqrt{u^2} \sqrt{u} \cdot \sqrt{v^4} \cdot \sqrt{v}$$

$$3\sqrt{7} \cdot u\sqrt{u} \cdot v^2\sqrt{v}$$

$$3uv^2\sqrt{7uv}$$

$$1^2 = 1$$

$$2^2 = 4$$

$$3^2 = 9$$

$$4^2 = 16$$

$$5^2 = 25$$

$$6^2 = 36$$

$$7^2 = 49$$

$$8^2 = 64$$

$$9^2 = 81$$

$$10^2 = 100$$

$$11^2 = 121$$

$$12^2 = 144$$

$$13^2 = 169$$

$$14^2 = 196$$

$$15^2 = 225$$

$$16^2 = 256$$

$$17^2 = 289$$

$$18^2 = 324$$

$$19^2 = 361$$

$$20^2 = 400$$

$$\frac{1\sqrt{3} + \sqrt{3}}{2\sqrt{3}}$$

$$\sqrt{5} + \sqrt{2} \neq \sqrt{7}$$

$$\frac{\sqrt{48}}{2} \neq \sqrt{24}$$

$$\sqrt{48} = 4\sqrt{3}$$

$$\frac{4-4\sqrt{3}}{2}$$

$$\frac{4}{2} - \frac{4}{2}\sqrt{3}$$

$$\sqrt{\frac{a}{b}} \Leftrightarrow \frac{\sqrt{a}}{\sqrt{b}}$$

$$\frac{3\sqrt{5}}{4\sqrt{5}}$$

Simplify:

$$3 + \sqrt{32}$$

$$3 + \sqrt{16 \cdot 2}$$

$$3 + 4\sqrt{2}$$

$$\frac{4-\sqrt{48}}{2}$$

$$\frac{4-4\sqrt{3}}{2}$$

$$2-2\sqrt{3}$$

$$\frac{16}{5}$$

$$2 - \frac{6}{5}\sqrt{2}$$

$$\frac{5+\sqrt{75}}{5}$$

$$\frac{10-6\sqrt{2}}{5}$$

$$2 - \frac{6}{5}\sqrt{2}$$

$$\frac{2-\sqrt{98}}{2}$$

$$\frac{6-3\sqrt{5}}{3}$$

$$2 - \sqrt{5}$$

Using the Quotient Property to Simplify

$$\sqrt{\frac{9}{16}} = \frac{\sqrt{9}}{\sqrt{16}} = \frac{3}{4}$$

$$\sqrt{\frac{25}{16}} = \frac{5}{4}$$

$$\sqrt{\frac{49}{81}} = \frac{7}{9}$$

$$\sqrt{\frac{45}{80}} = \sqrt{\frac{9}{16}} = \frac{3}{4}$$

$$\sqrt{\frac{75}{48}} = \sqrt{\frac{25}{16}} = \frac{5}{4}$$

$$\sqrt{\frac{98}{162}} = \sqrt{\frac{49}{81}} = \frac{7}{9}$$

$$\sqrt{\frac{m^6}{m^4}} = \sqrt{m^2} = m$$

$$\sqrt{\frac{x^{14}}{x^{10}}} = \sqrt{x^4} = x^2$$

$$\sqrt{\frac{48p^7}{3p^3}} = \sqrt{16p^4} = 4p^2$$

$$\sqrt{\frac{75z^5}{3z}} \quad \sqrt{\frac{72b^{12}}{2b^{10}}}$$

5z<sup>2</sup>

6b

Quotient Property of Square Roots

If a, b are non-negative real numbers and  $b \neq 0$ , then

$$\sqrt{\frac{a}{b}} = \frac{\sqrt{a}}{\sqrt{b}}$$

Simplify

$$\begin{aligned} \sqrt{\frac{21}{64}} &= \frac{\sqrt{21}}{\sqrt{64}} & \sqrt{\frac{19}{49}} &= \frac{\sqrt{19}}{\sqrt{49}} & \sqrt{\frac{28}{81}} &= \frac{\sqrt{28}}{\sqrt{81}} \\ &= \frac{\sqrt{21}}{8} & &= \frac{\sqrt{19}}{7} & &= \frac{2\sqrt{7}}{9} \end{aligned}$$

$$\begin{aligned} \sqrt{\frac{27m^3}{196}} & \quad \sqrt{\frac{48x^5}{100}} & \quad \sqrt{\frac{45x^5}{y^4}} \\ \sqrt{27} = 3\sqrt{3} & \quad \frac{4x^2\sqrt{3x}}{10} & \quad \frac{3x^2\sqrt{5x}}{y^2} \\ \sqrt{m^3} = m\sqrt{m} & \quad \frac{2x^2\sqrt{3x}}{5} & \\ \frac{3m\sqrt{3m}}{14} & \quad \sqrt{\frac{50x^5y^3}{72x^4y}} & \quad \sqrt{\frac{48m^7n^2}{125m^5n^9}} \end{aligned}$$

$$\begin{aligned} \sqrt{\frac{81d^4}{25}} & \quad \sqrt{\frac{25xy^2}{36}} & \quad \sqrt{\frac{48m^2}{125n^7}} \\ \frac{9d^2}{5} & \quad \frac{5y\sqrt{x}}{6} & \quad \frac{\sqrt{48m^2}}{\sqrt{125n^7}} \\ & & \quad \frac{4m\sqrt{3}}{5n^3\sqrt{5n}} \end{aligned}$$